

ANALYSIS FOR AN EXPERIMENT DESIGNED AS AUGMENTED LATTICE SQUARE DESIGN

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Abstract: SAS PROC GLM and SAS PROC MIXED procedures are given for analyzing data from experiments designed as augmented lattice square designs. A trend analysis using polynomial regression functions of row and column orders and interactions of these regressions. Higher ordered polynomial regressions are useable in the analysis as the number of rows and columns increase.

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Title: Analysis for an Experiment Designed as Augmented Lattice Square Design

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Importance: Augmented experiment designs are used internationally for screening the large number of new genotypes used in plant breeding programs. Any experiment design (complete block, incomplete block, row-column, or other) may be selected for the check or standard treatments replicated r times each. Then the blocks, incomplete blocks, or rows and columns are enlarged to accommodate the new treatments usually included in only one plot. The lattice square experiment design controls variation within each complete block in two directions (rows and columns). Augmented lattice square experiment designs (ALSDs) are easily constructed as described by Federer, W. T. (2000). Construction and analysis of an augmented lattice square design. Technical Report BU-1490-M, Department of Biometrics, Cornell University. ALSDs can accommodate $c = 2k$ or $3k$ check or standard cultivars in $r = k$ complete blocks and $n = k^2(k - 2)$ or $k^2(k - 3)$ new genotypes. An ALSD with $k = 4 = r$, $c = 8$, and $n = 32$ is used to illustrate a statistical analysis. A trend analysis using polynomial regression is used. The file name for this data set is auglsd.dat, and the data are presented below for the 64 responses.

| | | | | |
|---|---|---|----|----|
| 1 | 1 | 1 | 33 | 17 |
| 1 | 1 | 2 | 1 | 9 |
| 1 | 1 | 3 | 2 | 9 |
| 1 | 1 | 4 | 40 | 23 |
| 1 | 2 | 1 | 37 | 21 |
| 1 | 2 | 2 | 34 | 18 |
| 1 | 2 | 3 | 3 | 9 |
| 1 | 2 | 4 | 4 | 9 |
| 1 | 3 | 1 | 5 | 9 |
| 1 | 3 | 2 | 38 | 22 |
| 1 | 3 | 3 | 35 | 19 |
| 1 | 3 | 4 | 6 | 9 |
| 1 | 4 | 1 | 7 | 9 |
| 1 | 4 | 2 | 8 | 19 |
| 1 | 4 | 3 | 39 | 23 |
| 1 | 4 | 4 | 36 | 20 |
| 2 | 1 | 1 | 33 | 17 |
| 2 | 1 | 2 | 9 | 8 |
| 2 | 1 | 3 | 10 | 8 |
| 2 | 1 | 4 | 39 | 25 |
| 2 | 2 | 1 | 40 | 22 |
| 2 | 2 | 2 | 34 | 18 |
| 2 | 2 | 3 | 11 | 18 |
| 2 | 2 | 4 | 12 | 18 |
| 2 | 3 | 1 | 13 | 18 |
| 2 | 3 | 2 | 37 | 23 |
| 2 | 3 | 3 | 35 | 19 |
| 2 | 3 | 4 | 14 | 17 |
| 2 | 4 | 1 | 15 | 16 |
| 2 | 4 | 2 | 16 | 21 |
| 2 | 4 | 3 | 38 | 25 |
| 2 | 4 | 4 | 36 | 20 |
| 3 | 1 | 1 | 33 | 24 |
| 3 | 1 | 2 | 17 | 17 |
| 3 | 1 | 3 | 18 | 17 |

```

3 1 4 38 18
3 2 1 39 22
3 2 2 34 12
3 2 3 19 17
3 2 4 20 16
3 3 1 21 17
3 3 2 40 25
3 3 3 35 15
3 3 4 22 17
3 4 1 23 17
3 4 2 24 17
3 4 3 37 15
3 4 4 36 15
4 1 1 33 28
4 1 2 25 20
4 1 3 26 20
4 1 4 37 25
4 2 1 38 29
4 2 2 34 22
4 2 3 27 26
4 2 4 28 26
4 3 1 29 16
4 3 2 39 32
4 3 3 35 25
4 3 4 30 26
4 4 1 31 16
4 4 2 32 16
4 4 3 40 25
4 4 4 36 30

```

The SAS/GLM and SAS/MIXED codes for this data set are:

```

options ls = 76;
proc iml;
  opn3= orpol(1:4,2); /* The 4 is the number of columns and 2 indicates that
    linear and quadratic polynomial regression coefficients are desired. */
  opn3[,1]= (1:4)`;
  op3 =opn3 ;      print op3; /* Print-out of coefficients. */
  create opn3 from opn3[colname ={'COL' 'C1' 'C2'}]; append from opn3;
  close  opn3;run;
  opn4 =orpol(1:4,2); /* There are 4 rows and two regressions. */
  opn4[,1]=(1:4)` ;
  op4 =opn4;      print op4;
  create opn4 from opn4[colname ={'ROW' 'R1' 'R2'}]; append from opn4;
  close opn4; run;
data auglsd8;
  infile 'auglsd8.dat';
  input rep row col trt yield;
  if (trt>32) then new = 0; else new = 1;
  /* This divides the 40 entries into 32 new treatments which are
  considered as random effects and 8 checks which are fixed effects. */
  if (new) then trtn = 999; else trtn = trt;
data augbig;set auglsd8;
  /* The regression coefficients are added to the data set. */
  idx = _n_; run;
proc sort data = augbig;
  by COL; run;data augbig; merge augbig opn3; by COL; run;

```

```

proc sort data = augbig;
  by ROW; run; data augbig; merge augbig opn4; by ROW; run;
proc sort data = augbig; by idx; run;
proc glm data = augbig;
  class row col trt trtn rep;
  model yield = rep trt C1*rep R1*rep C1*R1*rep;
  lsmeans trt/out = lsmeans noprint; run;
proc sort data = lsmeans; by descending lsmean;
/* n is usually quite large and this statement arranges the fixed
effect means in descending order for viewing. */
proc print; run;
proc mixed data = augbig;
  class rep row col trt trtn;
  model yield = trtn/solution;
  random rep C1*rep R1*rep C1*R1*rep trt*new/solution;
/* These two statements obtain solutions for the various effects. */
  lsmeans trtn; make 'solutionr' out = sr noprint; run;
proc sort data = sr;
  by descending _est_;
/*The effect solutions are arranged from largest to smallest. */
proc print; run;
quit;

```

The output for the above example and the above program is presented in a modified version of the actual print-out of the output. Below are the linear and quadratic coefficients:

```

OP3
  1 -0.67082      0.5
  2 -0.223607    -0.5
  3  0.2236068   -0.5
  4  0.6708204    0.5

```

```

OP4
  1 -0.67082      0.5
  2 -0.223607    -0.5
  3  0.2236068   -0.5
  4  0.6708204    0.5

```

```

Class Level Information
Class      Levels      Values
ROW         4          1 2 3 4
COL         4          1 2 3 4
TRT        40          1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21
                22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39
                40
TRTN         9          33 34 35 36 37 38 39 40 999
REP          4          1 2 3 4
Number of observations in data set = 64

```

| Dependent Variable: YIELD | | Sum of | Mean | | |
|---------------------------|----|------------|----------|---------|--------|
| Source | DF | Squares | Square | F Value | Pr > F |
| Model | 54 | 2022.63549 | 37.45621 | 5.73 | 0.0041 |
| Error | 9 | 58.84888 | 6.53876 | | |
| Corrected Total | 63 | 2081.48438 | | | |

| | | | |
|----------|----------|----------|------------|
| R-Square | C.V. | Root MSE | YIELD Mean |
| 0.971727 | 13.62652 | 2.55710 | 18.7656 |

Dependent Variable: YIELD

| Source | DF | Type I SS | Mean Square | F Value | Pr > F |
|-----------|----|-------------|-------------|---------|--------|
| REP | 3 | 634.92188 | 211.64063 | 32.37 | 0.0001 |
| TRT | 39 | 1284.68750 | 32.94071 | 5.04 | 0.0070 |
| C1*REP | 4 | 52.76528 | 13.19132 | 2.02 | 0.1755 |
| R1*REP | 4 | 3.38948 | 0.84737 | 0.13 | 0.9677 |
| C1*R1*REP | 4 | 46.87135 | 11.71784 | 1.79 | 0.2145 |
| Source | DF | Type III SS | Mean Square | F Value | Pr > F |
| REP | 3 | 240.67132 | 80.22377 | 12.27 | 0.0016 |
| TRT | 39 | 1066.10112 | 27.33593 | 4.18 | 0.0137 |
| C1*REP | 4 | 37.86878 | 9.46720 | 1.45 | 0.2953 |
| R1*REP | 4 | 23.77297 | 5.94324 | 0.91 | 0.4985 |
| C1*R1*REP | 4 | 46.87135 | 11.71784 | 1.79 | 0.2145 |

| Fixed effect means:OBS | | NAME | TRT | LSMEAN | STDERR |
|------------------------|--|-------|-----|---------|---------|
| 1 | | YIELD | 36 | 28.5625 | 3.98587 |
| 2 | | YIELD | 22 | 27.5443 | 3.87268 |
| 3 | | YIELD | 33 | 26.5625 | 3.98587 |
| 4 | | YIELD | 30 | 24.3923 | 3.87268 |
| 5 | | YIELD | 39 | 24.1171 | 1.67939 |
| 6 | | YIELD | 20 | 23.9249 | 3.40407 |
| 7 | | YIELD | 28 | 23.0745 | 3.40407 |
| 8 | | YIELD | 40 | 23.0142 | 1.67939 |
| 9 | | YIELD | 38 | 22.9711 | 1.67939 |
| 10 | | YIELD | 19 | 22.3609 | 2.89414 |
| 11 | | YIELD | 27 | 22.2280 | 2.89414 |
| 12 | | YIELD | 18 | 22.0455 | 3.40407 |
| 13 | | YIELD | 14 | 21.9964 | 3.87268 |
| 14 | | YIELD | 17 | 21.7855 | 3.87268 |
| 15 | | YIELD | 37 | 20.8976 | 1.67939 |
| 16 | | YIELD | 35 | 20.5625 | 1.41148 |
| 17 | | YIELD | 12 | 20.0757 | 3.40407 |
| 18 | | YIELD | 11 | 19.6544 | 2.89414 |
| 19 | | YIELD | 34 | 17.8125 | 1.41148 |
| 20 | | YIELD | 25 | 17.2728 | 3.87268 |
| 21 | | YIELD | 26 | 16.5147 | 3.40407 |
| 22 | | YIELD | 24 | 15.8193 | 5.01784 |
| 23 | | YIELD | 6 | 14.5671 | 3.87268 |
| 24 | | YIELD | 1 | 14.3972 | 3.87268 |
| 25 | | YIELD | 9 | 14.0444 | 3.87268 |
| 26 | | YIELD | 8 | 13.7216 | 5.01784 |
| 27 | | YIELD | 21 | 12.9400 | 5.01784 |
| 28 | | YIELD | 16 | 12.6102 | 5.01784 |
| 29 | | YIELD | 4 | 11.6749 | 3.40407 |
| 30 | | YIELD | 2 | 11.5900 | 3.40407 |
| 31 | | YIELD | 3 | 11.2568 | 2.89414 |
| 32 | | YIELD | 10 | 10.5998 | 3.40407 |
| 33 | | YIELD | 13 | 10.1342 | 5.01784 |
| 34 | | YIELD | 23 | 8.6472 | 8.44815 |
| 35 | | YIELD | 32 | 7.5988 | 5.01784 |
| 36 | | YIELD | 29 | 7.0391 | 5.01784 |
| 37 | | YIELD | 5 | 3.6367 | 5.01784 |
| 38 | | YIELD | 31 | 3.5431 | 8.44815 |
| 39 | | YIELD | 15 | -0.5431 | 8.44815 |

40 YIELD 7 -3.1472 8.44815

REML Estimation Iteration History

| Iteration | Evaluations | Objective | Criterion |
|-----------|-------------|--------------|------------|
| 0 | 1 | 245.77696870 | |
| 1 | 3 | 218.84012634 | 0.00762773 |
| 2 | 2 | 218.34805379 | 0.00012725 |
| 3 | 2 | 218.33482743 | 0.00000093 |
| 4 | 1 | 218.33472566 | 0.00000000 |

Convergence criteria met.

Covariance Parameter Estimates (REML)

| Cov Parm | Estimate |
|-----------|-------------|
| REP | 11.99469629 |
| C1*REP | 1.88018116 |
| R1*REP | 3.98577174 |
| C1*R1*REP | 4.69746155 |
| NEW*TRT | 5.87662721 |
| Residual | 8.41233535 |

Solution for Fixed Effects

| Effect | TRTN | Estimate | Std Error | DF | t | Pr > t |
|-----------|------|-------------|------------|----|------|---------|
| INTERCEPT | | 15.84932467 | 1.85872722 | 3 | 8.53 | 0.0034 |
| Effect | TRTN | Estimate | Std Error | DF | t | Pr > t |
| TRTN | 33 | 6.02505345 | 1.80689098 | 9 | 3.33 | 0.0087 |
| TRTN | 34 | 1.78104271 | 1.61807612 | 9 | 1.10 | 0.2996 |
| TRTN | 35 | 3.51473327 | 1.61757976 | 9 | 2.17 | 0.0578 |
| TRTN | 36 | 4.97612515 | 1.80199562 | 9 | 2.76 | 0.0221 |
| TRTN | 37 | 5.08850236 | 1.67222656 | 9 | 3.04 | 0.0140 |
| TRTN | 38 | 7.28885283 | 1.67222656 | 9 | 4.36 | 0.0018 |
| TRTN | 39 | 9.63215629 | 1.67222656 | 9 | 5.76 | 0.0003 |
| TRTN | 40 | 8.35433917 | 1.67222656 | 9 | 5.00 | 0.0007 |
| TRTN | 999 | 0.00000000 | . | . | . | . |

Least Squares Means (Check, fixed effect means.)

| Effect | TRTN | LSMEAN | Std Error | DF | t | Pr > t |
|--------|------|-------------|------------|----|-------|---------|
| TRTN | 33 | 21.87437812 | 2.39139410 | 9 | 9.15 | 0.0001 |
| TRTN | 34 | 17.63036738 | 2.26946107 | 9 | 7.77 | 0.0001 |
| TRTN | 35 | 19.36405795 | 2.26934312 | 9 | 8.53 | 0.0001 |
| TRTN | 36 | 20.82544982 | 2.38836997 | 9 | 8.72 | 0.0001 |
| TRTN | 37 | 20.93782703 | 2.31267932 | 9 | 9.05 | 0.0001 |
| TRTN | 38 | 23.13817750 | 2.31267932 | 9 | 10.00 | 0.0001 |
| TRTN | 39 | 25.48148096 | 2.31267932 | 9 | 11.02 | 0.0001 |
| TRTN | 40 | 24.20366385 | 2.31267932 | 9 | 10.47 | 0.0001 |
| TRTN | 999 | 15.84932467 | 1.85872722 | 9 | 8.53 | 0.0001 |

(Solutions for random effects arranged in descending order. To obtain the means, add the intercept value to each of the effects below.)

| OBS | EFFECT | REP | TRT | EST | SEPRED | DF | T | PT |
|-----|---------|-----|-----|------------|------------|----|------|--------|
| 1 | REP | 4 | | 4.85091339 | 1.86295604 | 9 | 2.60 | 0.0286 |
| 2 | R1*REP | 2 | | 2.51920549 | 1.33546047 | 9 | 1.89 | 0.0919 |
| 3 | NEW*TRT | | 8 | 2.16475642 | 1.94313336 | 9 | 1.11 | 0.2941 |
| 4 | NEW*TRT | | 27 | 2.01517588 | 1.90869357 | 9 | 1.06 | 0.3186 |
| 5 | NEW*TRT | | 28 | 1.85527717 | 1.93230928 | 9 | 0.96 | 0.3621 |

| | | | | | | | | |
|----|-----------|---|----|-------------|------------|---|-------|--------|
| 6 | NEW*TRT | | 30 | 1.81072275 | 1.93311801 | 9 | 0.94 | 0.3734 |
| 7 | C1*R1*REP | 4 | | 1.73101272 | 1.85245416 | 9 | 0.93 | 0.3745 |
| 8 | NEW*TRT | | 16 | 1.54679253 | 1.94313336 | 9 | 0.80 | 0.4465 |
| 9 | NEW*TRT | | 22 | 1.54645580 | 1.93311801 | 9 | 0.80 | 0.4443 |
| 10 | C1*REP | 4 | | 1.25643193 | 1.09118038 | 9 | 1.15 | 0.2792 |
| 11 | NEW*TRT | | 24 | 1.25209662 | 1.94313336 | 9 | 0.64 | 0.5354 |
| 12 | NEW*TRT | | 11 | 1.23086038 | 1.90869357 | 9 | 0.64 | 0.5351 |
| 13 | NEW*TRT | | 19 | 1.17618212 | 1.90869357 | 9 | 0.62 | 0.5530 |
| 14 | NEW*TRT | | 12 | 1.11283909 | 1.93230928 | 9 | 0.58 | 0.5788 |
| 15 | NEW*TRT | | 18 | 1.01457415 | 1.94260482 | 9 | 0.52 | 0.6141 |
| 16 | R1*REP | 1 | | 1.01019332 | 1.33546047 | 9 | 0.76 | 0.4687 |
| 17 | NEW*TRT | | 23 | 1.00479517 | 1.99102006 | 9 | 0.50 | 0.6259 |
| 18 | NEW*TRT | | 20 | 0.93494169 | 1.93230928 | 9 | 0.48 | 0.6400 |
| 19 | NEW*TRT | | 21 | 0.92045869 | 1.93273116 | 9 | 0.48 | 0.6452 |
| 20 | NEW*TRT | | 17 | 0.88317994 | 1.94374142 | 9 | 0.45 | 0.6603 |
| 21 | NEW*TRT | | 13 | 0.83974581 | 1.93273116 | 9 | 0.43 | 0.6742 |
| 22 | NEW*TRT | | 14 | 0.40203254 | 1.93311801 | 9 | 0.21 | 0.8399 |
| 23 | C1*REP | 2 | | 0.34480113 | 1.09118038 | 9 | 0.32 | 0.7592 |
| 24 | C1*R1*REP | 1 | | 0.28936528 | 1.85245416 | 9 | 0.16 | 0.8793 |
| 25 | NEW*TRT | | 33 | 0.00000000 | 2.42417557 | 9 | 0.00 | 1.0000 |
| 26 | NEW*TRT | | 34 | 0.00000000 | 2.42417557 | 9 | 0.00 | 1.0000 |
| 27 | NEW*TRT | | 35 | 0.00000000 | 2.42417557 | 9 | 0.00 | 1.0000 |
| 28 | NEW*TRT | | 36 | 0.00000000 | 2.42417557 | 9 | 0.00 | 1.0000 |
| 29 | NEW*TRT | | 37 | 0.00000000 | 2.42417557 | 9 | 0.00 | 1.0000 |
| 30 | NEW*TRT | | 38 | 0.00000000 | 2.42417557 | 9 | 0.00 | 1.0000 |
| 31 | NEW*TRT | | 39 | 0.00000000 | 2.42417557 | 9 | 0.00 | 1.0000 |
| 32 | NEW*TRT | | 40 | 0.00000000 | 2.42417557 | 9 | 0.00 | 1.0000 |
| 33 | C1*REP | 1 | | -0.02662262 | 1.09118038 | 9 | -0.02 | 0.9811 |
| 34 | REP | 2 | | -0.42232220 | 1.86295604 | 9 | -0.23 | 0.8257 |
| 35 | C1*R1*REP | 3 | | -0.46971222 | 1.85245416 | 9 | -0.25 | 0.8055 |
| 36 | NEW*TRT | | 25 | -0.53275905 | 1.94374142 | 9 | -0.27 | 0.7902 |
| 37 | NEW*TRT | | 26 | -0.55027490 | 1.94260482 | 9 | -0.28 | 0.7834 |
| 38 | NEW*TRT | | 15 | -0.60995214 | 1.99102006 | 9 | -0.31 | 0.7663 |
| 39 | R1*REP | 3 | | -0.77362810 | 1.33546047 | 9 | -0.58 | 0.5766 |
| 40 | R1*REP | 4 | | -0.91895723 | 1.33546047 | 9 | -0.69 | 0.5087 |
| 41 | NEW*TRT | | 31 | -1.01254232 | 1.99102006 | 9 | -0.51 | 0.6233 |
| 42 | C1*REP | 3 | | -1.02947994 | 1.09118038 | 9 | -0.94 | 0.3701 |
| 43 | C1*R1*REP | 2 | | -1.32767888 | 1.85245416 | 9 | -0.72 | 0.4917 |
| 44 | NEW*TRT | | 2 | -1.38564933 | 1.94260482 | 9 | -0.71 | 0.4937 |
| 45 | NEW*TRT | | 29 | -1.39513647 | 1.93273116 | 9 | -0.72 | 0.4887 |
| 46 | NEW*TRT | | 1 | -1.42624812 | 1.94374142 | 9 | -0.73 | 0.4818 |
| 47 | NEW*TRT | | 32 | -1.45720674 | 1.94313336 | 9 | -0.75 | 0.4724 |
| 48 | NEW*TRT | | 4 | -1.56655327 | 1.93230928 | 9 | -0.81 | 0.4384 |
| 49 | NEW*TRT | | 3 | -1.58335059 | 1.90869357 | 9 | -0.83 | 0.4282 |
| 50 | REP | 3 | | -1.67547560 | 1.86295604 | 9 | -0.90 | 0.3919 |
| 51 | NEW*TRT | | 5 | -1.76704354 | 1.93273116 | 9 | -0.91 | 0.3844 |
| 52 | NEW*TRT | | 6 | -1.78805600 | 1.93311801 | 9 | -0.92 | 0.3791 |
| 53 | NEW*TRT | | 7 | -1.91714185 | 1.99102006 | 9 | -0.96 | 0.3608 |
| 54 | NEW*TRT | | 9 | -2.24587207 | 1.94374142 | 9 | -1.16 | 0.2777 |
| 55 | NEW*TRT | | 10 | -2.47310037 | 1.94260482 | 9 | -1.27 | 0.2349 |
| 56 | REP | 1 | | -2.75311559 | 1.86295604 | 9 | -1.48 | 0.1736 |